

Closed book. No calculators are to be used for this quiz.
Quiz duration: 10 minutes

Name: SOLUTION

Student ID:

Signature:

A sinusoidal sound wave has the speed v and wave length λ . The sound wave travels in the positive x - direction and at $(t=0, x=0)$ it has maximum upward displacement of A . Write the corresponding displacement $y(x,t)$ and pressure $p(x,t)$ wave equations in terms of (v, λ, A) describing the same wave. (Take the bulk modulus of the medium as B .)

$$y(x,t) = A \cos(kx - \omega t) \quad \rightarrow \text{positive } \hat{x} \text{ direction}$$

$$k = \frac{2\pi}{\lambda}, \quad \lambda f = v$$

$$\omega = 2\pi f = 2\pi \cdot \frac{v}{\lambda}$$

$$(I) \quad y(x,t) = A \cos \left[\frac{2\pi}{\lambda} (x - vt) \right] \quad \checkmark$$

$$(II) \quad p(x,t) = -B \frac{\partial y}{\partial x} = -B A \left(-\sin \left[\frac{2\pi}{\lambda} (x - vt) \right] \right) \cdot \frac{2\pi}{\lambda}$$
$$= \frac{2\pi}{\lambda} B A \sin \left[\frac{2\pi}{\lambda} (x - vt) \right] \quad \checkmark$$

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The pressure in a traveling sound wave is given by the equation

$$P = (1.5 \text{ Pa}) \sin \pi [(1.00 \text{ m}^{-1})x - (330 \text{ s}^{-1})t]$$

Find; a) the pressure amplitude, b) the frequency, c) the wavelength and d) the speed of the wave.

$$(a) \quad p(x,t) = B A k \sin(kx - \omega t)$$

$$B A k = 1.5 \text{ Pa}$$

$$A = \frac{1.5 \text{ Pa}}{B k} = \frac{1.5}{\pi B} \approx \frac{1}{2B}$$

$$(b) \quad \omega = 2\pi f = 330\pi \quad f = 115 \text{ Hz}$$

$$(c) \quad \lambda = \frac{2\pi}{k}, \quad k = \pi, \quad \lambda = 2 \text{ m}$$

$$(d) \quad v = \lambda f = 115.2 = 330 \text{ m/s}$$

Section 3

Quiz 12

06 January 2011

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Name: SOLUTION

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Signature:

Calculate the length of an organ pipe that is open at one end and closed at the other if its fundamental frequency is to be 9 times that of a pipe that is 7 m. long and open at both ends.

both
Open / $f_n = \frac{nv}{2L} = \frac{nv}{2 \cdot 7}$

one end
open / $f_n' = \frac{nv}{4L} = 9f_n = 9 \cdot \frac{nv}{14} = \frac{nv}{4L}$

$$L = \frac{14}{4 \cdot 9} = \frac{14}{36} = \frac{7}{18} \text{ m}$$

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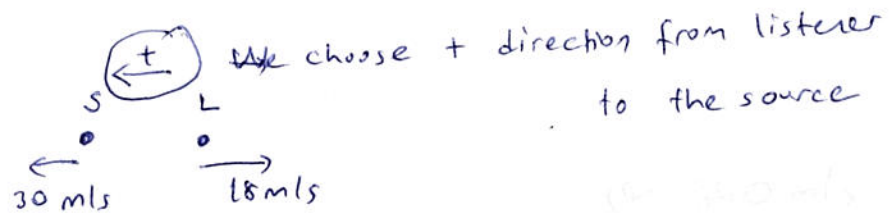
Name: SOLUTION

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Signature:

A railroad train is traveling at 30 m/s in still air. The frequency of the note emitted by the train whistle is 200 Hz. What frequency is heard by a passenger on a train moving in the opposite direction to the first at 18 m/s and moving away from the first? (Listener and source are moving away from each other!) The speed of sound is 340 m/s.

$$f_L = \left(\frac{v + v_L}{v + v_S} \right) f_S \quad v: 340 \text{ m/s}$$



$$f_L = \left(\frac{340 - 18}{340 + 30} \right) \cdot 200 \text{ Hz}$$

$$= (0.87) (200) \text{ Hz}$$

$$f_L < f_S$$

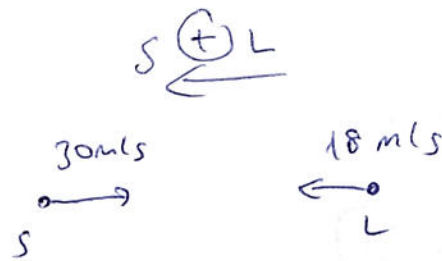
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A railroad train is traveling at 30 m/s in still air. The frequency of the note emitted by the train whistle is 200 Hz. What frequency is heard by a passenger on a train moving in the opposite direction to the first at 18 m/s and approaching the first? (Listener and source are approaching each other!) The speed of sound is 340 m/s.



$$v = 340 \text{ m/s}$$

$$f_L = \left(\frac{v + v_L}{v + v_S} \right) f_S$$

$$= \left(\frac{v + 18}{v - 30} \right) f_S = \left(\frac{340 + 18}{340 - 30} \right) 200 \text{ Hz.}$$

$$= (1.15)(200) \text{ Hz.}$$

$$f_L > f_S$$